

# **Non-parametric investigation of the Kuznets hypothesis for transitional countries**

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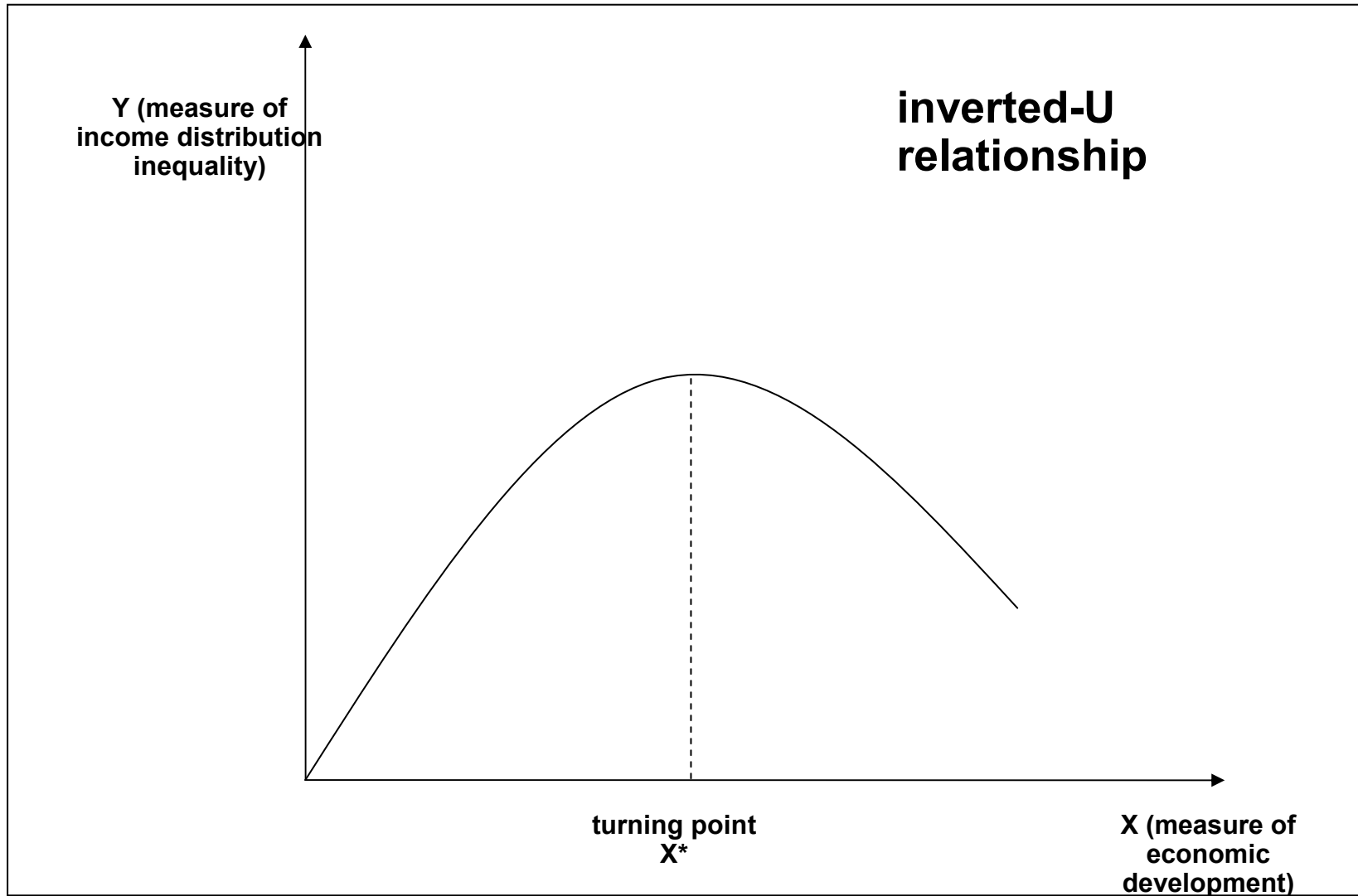
NUMBER ONE

### ECONOMIC GROWTH AND INCOME INEQUALITY\*

*By* SIMON KUZNETS

The central theme of this paper is the character and causes of long-term changes in the personal distribution of income. Does inequality in the distribution of income increase or decrease in the course of a country's economic growth? What factors determine the secular level and trends of income inequalities?

# The Kuznets hypothesis



## Verification of the Kuznets hypothesis

- **Ahluwalia M. (1976), “Income distribution and development”,**
- **Barro R. (2000), “Inequality and growth in a panel of countries”,**
- **Ho-Chuan River Huang (2004), “A flexible nonlinear inference to the Kuznets hypothesis”,**
- **Mushinski D.(2001), “Using non-parametrics to inform parametric tests of Kuznets’ hypothesis”,**
- **Papanek G. and Kyn O. (1986), “The effect on income distribution of development, the growth rate and economic strategy”,**
- **Savvides A. and Stengos T. (2000), “Income inequality and economic development: evidence from the threshold regression model”,**
- **Sukiassyan G. (2007), “Inequality and growth: What does the transition economy data say?”**

# Variables

## **Inequality measures:**

- **Gini index**
- **Ratio of incomes richest 10% to poorest 10%**
- **Ratio of income incomes richest 20% to poorest 20%**

## **Measure of economic development:**

- **GDP per capita PPP US\$**
- **Growth rate of GDP**
- **Literacy rate**
- **Secondary school enrollment**

## Objectives

- **To test the Kuznets hypothesis on the theoretical level,**
- **To determine the conditions on which the inverted-U dependence of the Gini index on the mean income might take place,**
- **To give an economic interpretation of the obtained mathematical results,**
- **To test whether the Kuznets hypothesis is valid for countries with transition economy.**

## Theoretical approach

The Gini index is a function of  $n$  variables:

$$G = \left( 1 - \frac{1}{n} - 2 \frac{n-1}{n^2} \cdot \frac{X_1}{Z} - 2 \frac{n-2}{n^2} \cdot \frac{X_2}{Z} - \dots - \frac{2}{n^2} \cdot \frac{X_{n-1}}{Z} \right) \cdot 100\%$$

$n$  – quantity of income groups,

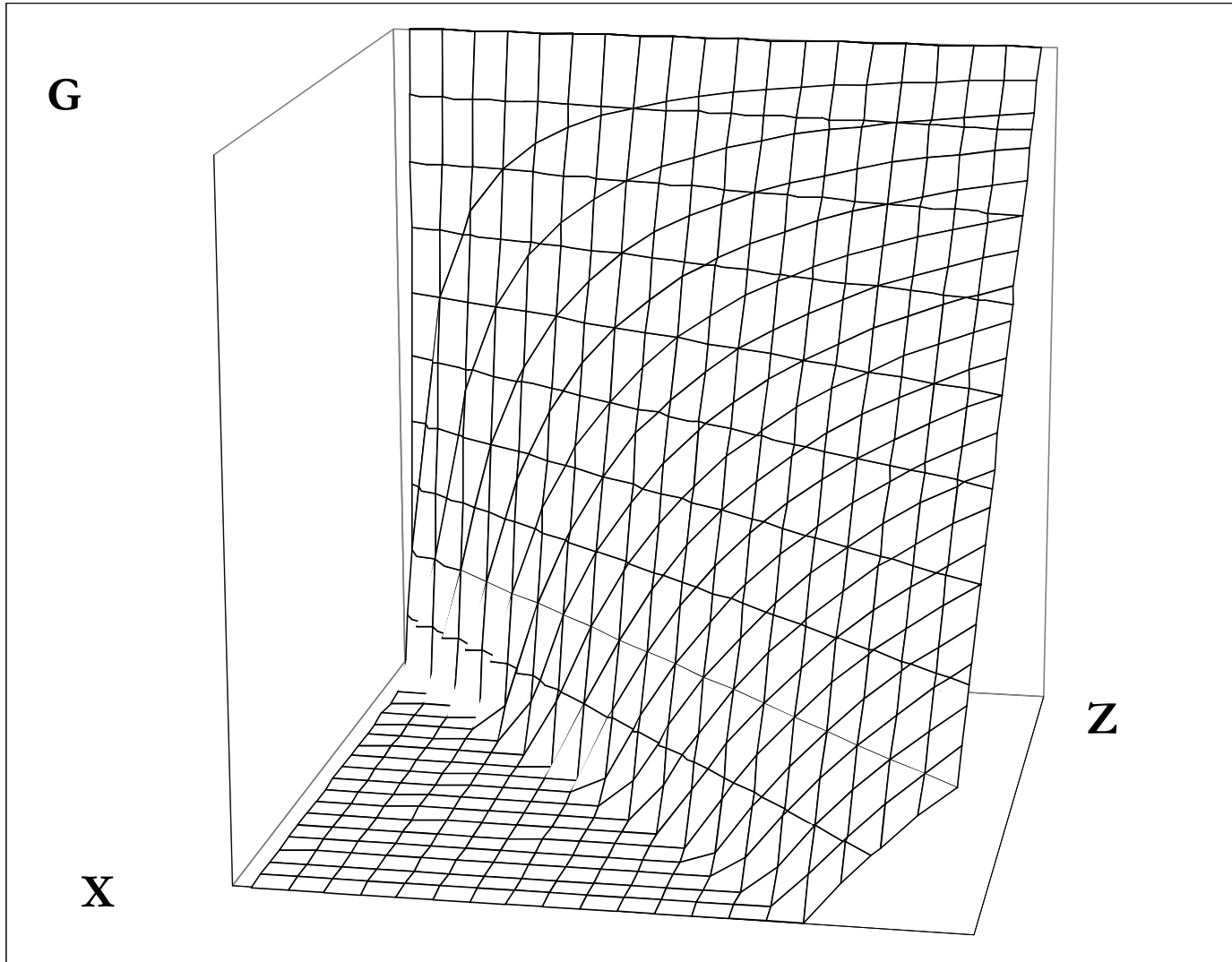
$G$  – the Gini index,

$X_1$  - the income of the poorest group,

$X_n$  - the income of the richest group,

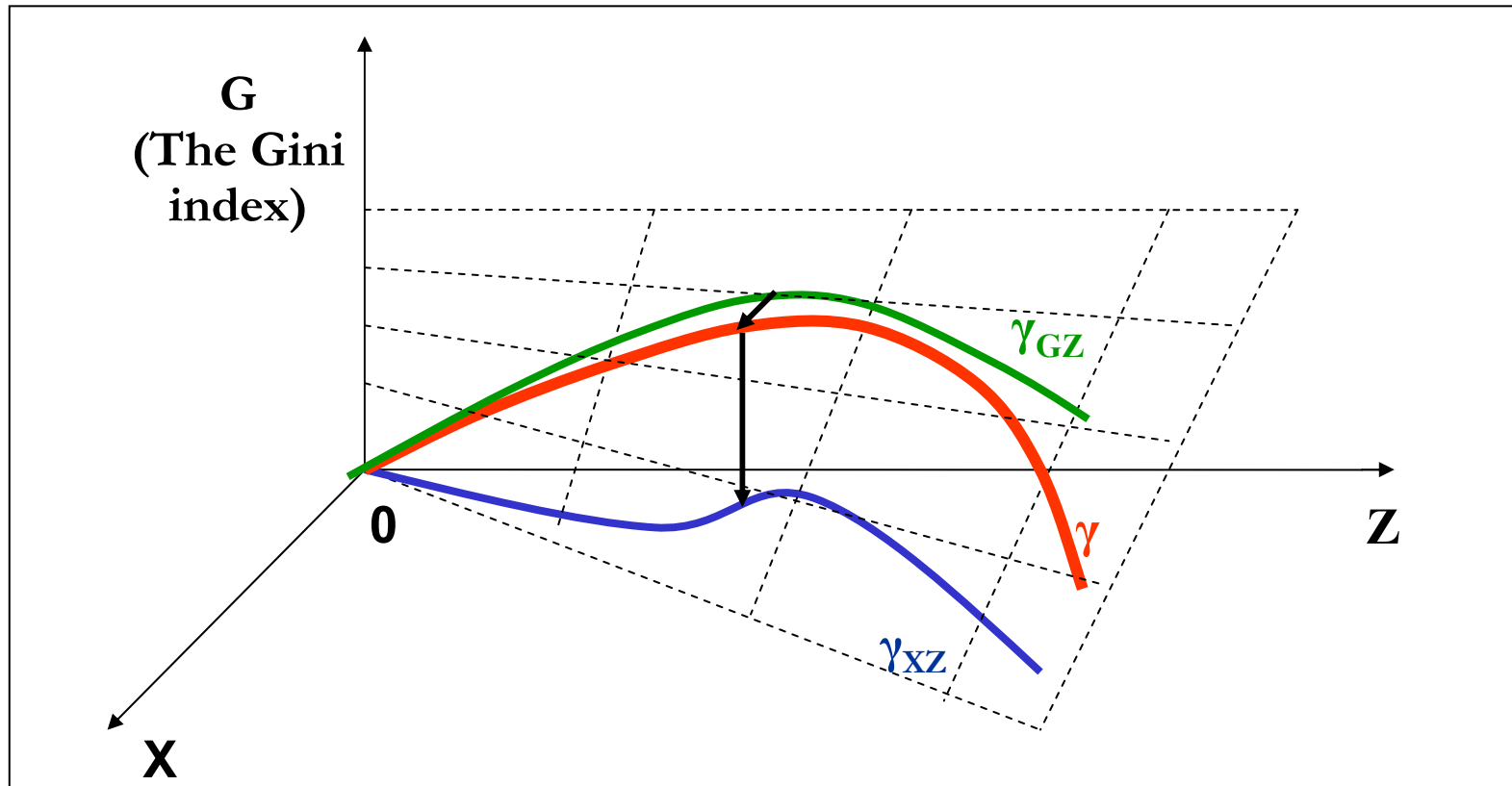
$Z$  - the mean income

# Manifold

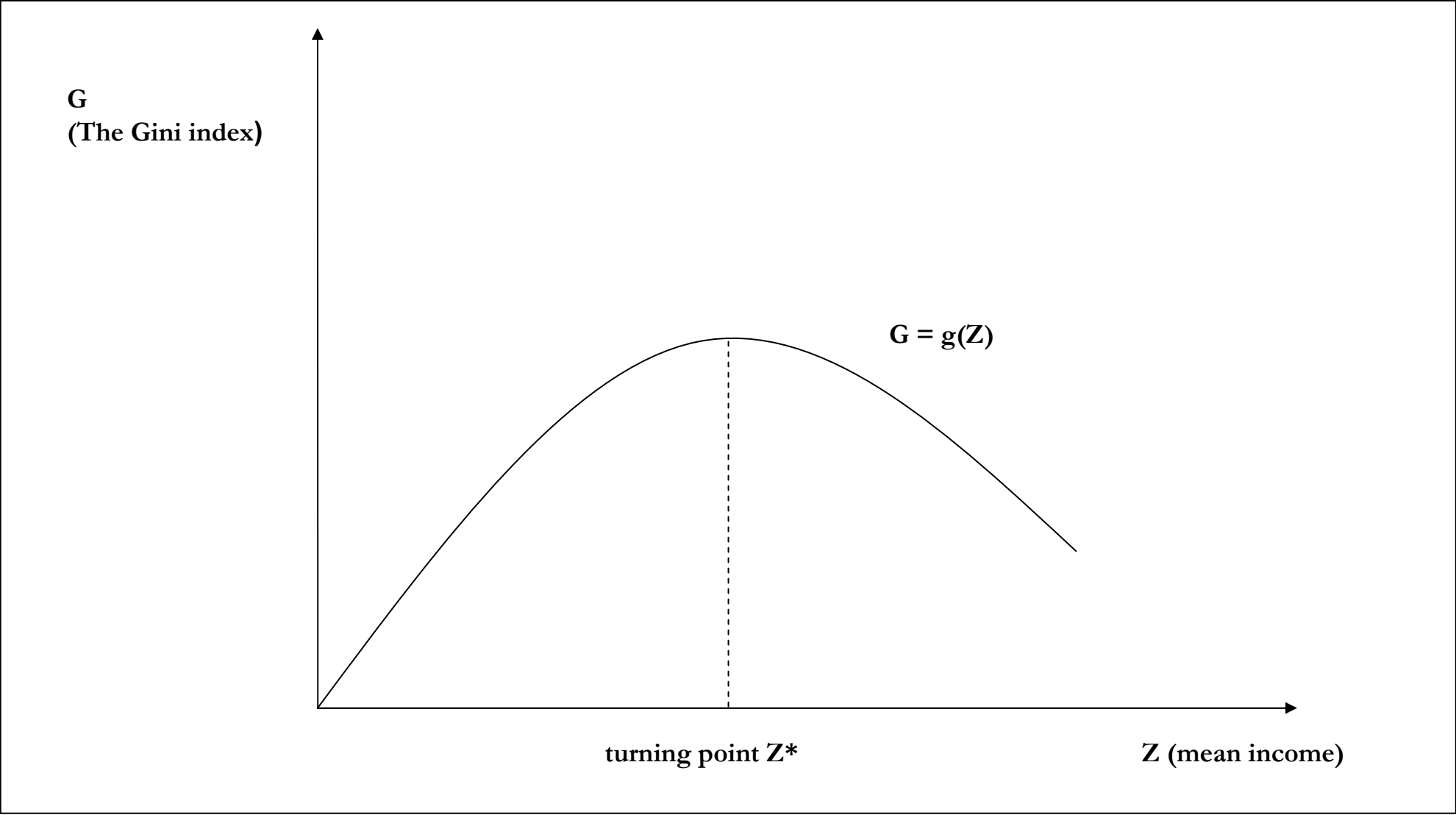




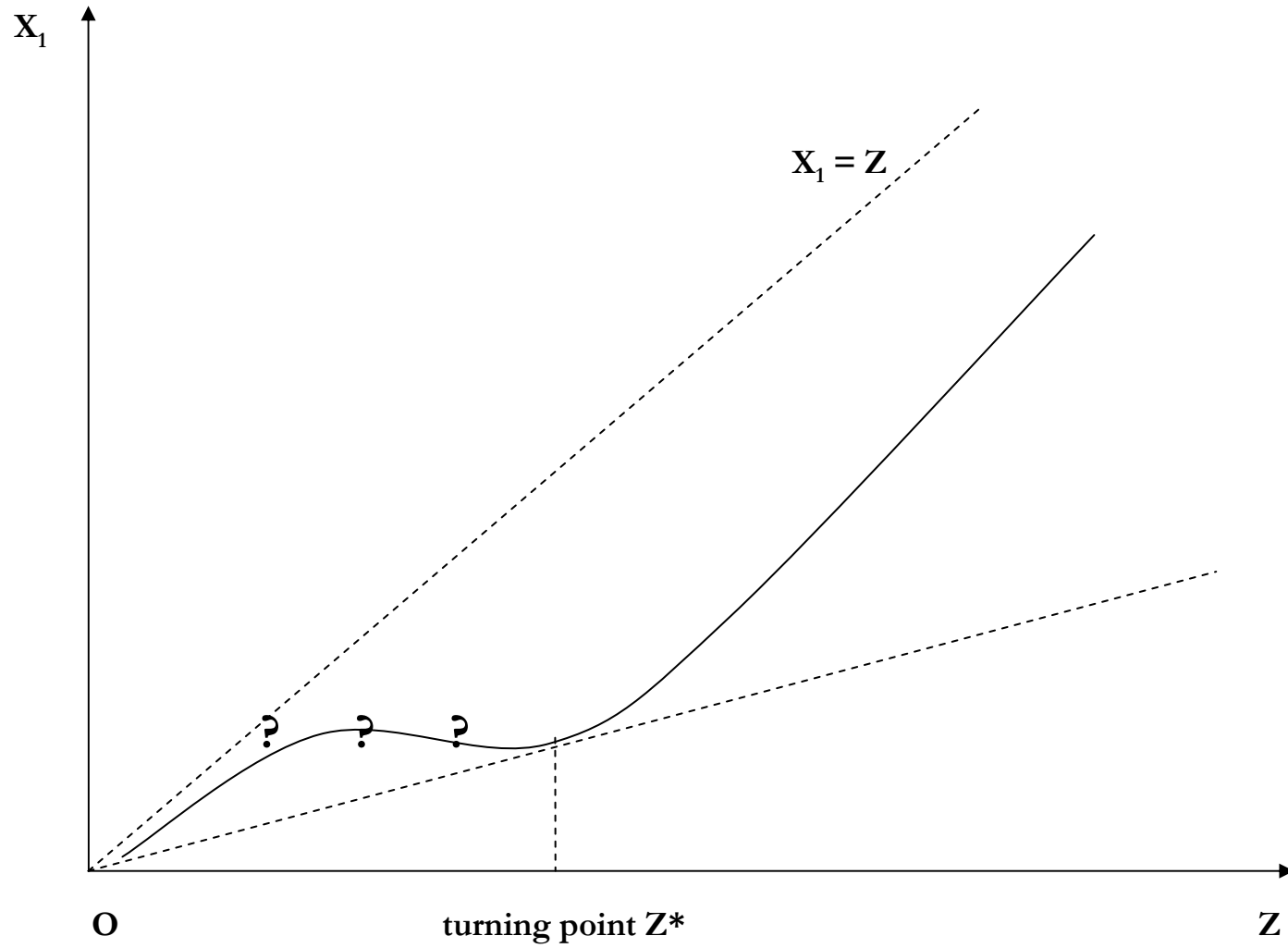
# Projections



# Projection onto the plane GOZ



# Projection onto the plane $X_1OZ$



## Main theoretical result

**The drop in the Gini index after reaching the turning point is possible only with the low-income groups' income growth being ahead**

## The Gini index is a function of share incomes

$$G = \left( 1 - \frac{1}{n} - 2 \frac{n-1}{n} \cdot p_1 - 2 \frac{n-2}{n} \cdot p_2 - \dots - \frac{2}{n} \cdot p_{n-1} \right) \cdot 100\%$$

**n** – quantity of income groups,

**G** – the Gini index,

**p<sub>i</sub>** - is the income share of i-th group,  $i = 1, \dots, n$ .

If **n = 5**, then

$$G = 100\% \cdot (0.8 - 1.6 p_1 - 1.2 p_2 - 0.8 p_3 - 0.4 p_4)$$

If **G** has inverted – U form as a function of **Z** (mean income), then  $p_1, \dots, p_n$  (income shares) have U – form as the functions of **Z** .

## **Source of data**

**Human development report 2006**

**Published for the United Nations**

**Development Programme**

**(UNDP)**

**29 countries with transition economy**

## Empirical results. Parametric specification

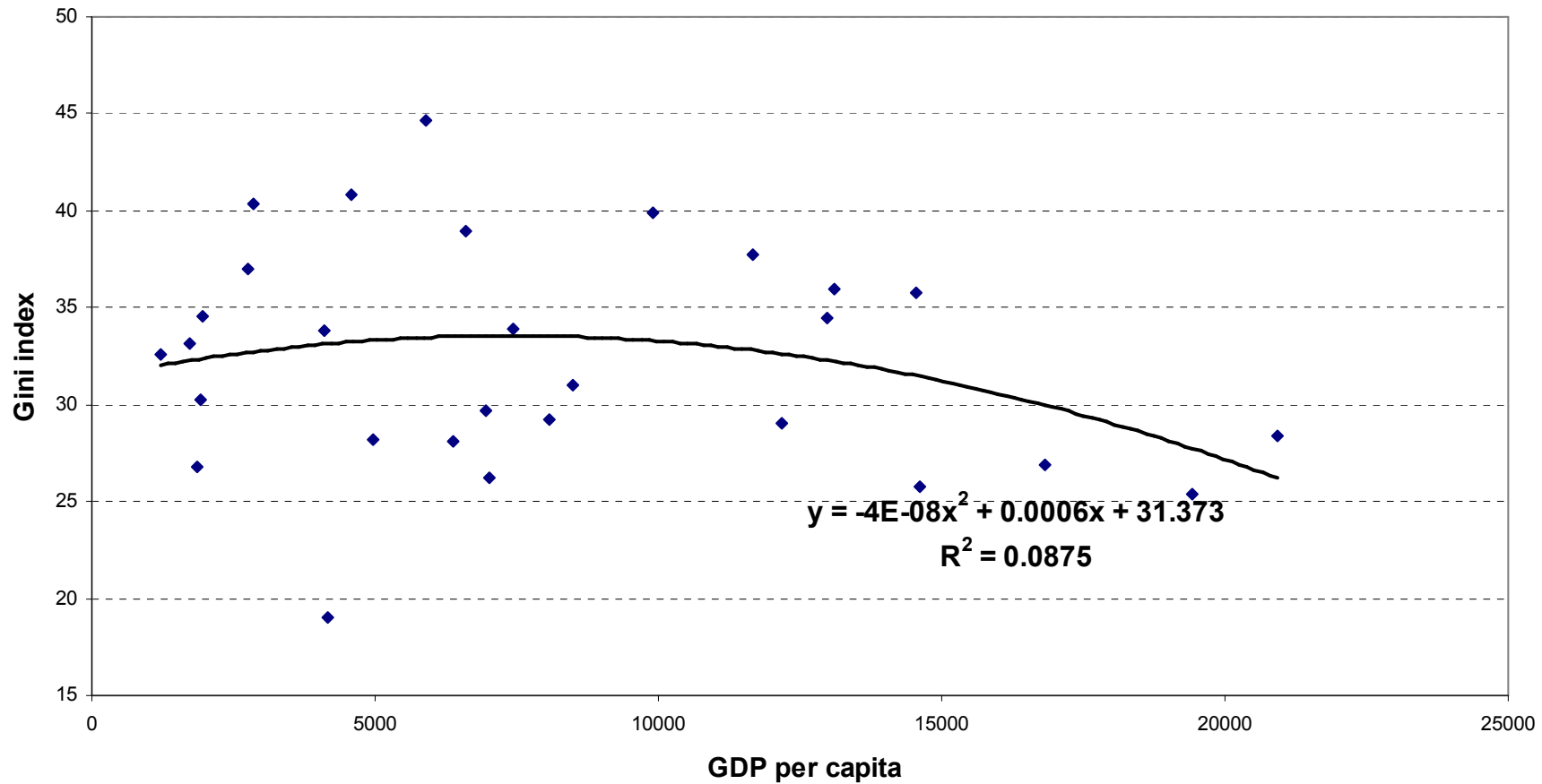
$$GINI = \beta_0 + \beta_1 GDP + \beta_2 GDP^2 + \varepsilon$$

**Table 1. Regression of the Gini index on per capita GDP and its squared term**

Source	SS	df	MS	Number of obs = 29	F( 2, 26) = 1.25
Model	81.6520979	2	40.8260489	Prob > F = 0.3041	
Residual	851.578306	26	32.7530118	R-squared = 0.0875	
				Adj R-squared = 0.0173	
Total	933.230404	28	33.3296573	Root MSE = 5.723	
GINI	Coef.	Std. Err.	t	P>t	[95% Conf. Interval]
GDP	.00059	.0007261	0.81	0.424	-.0009024 .0020825
GDP2	-4.00e-08	3.49e-08	-1.15	0.262	-1.12e-07 3.17e-08
_cons	31.37331	3.020073	10.39	0.000	25.16546 37.58116

# Empirical results. Parametric specification

Transitionan countries





## Nonparametric specification

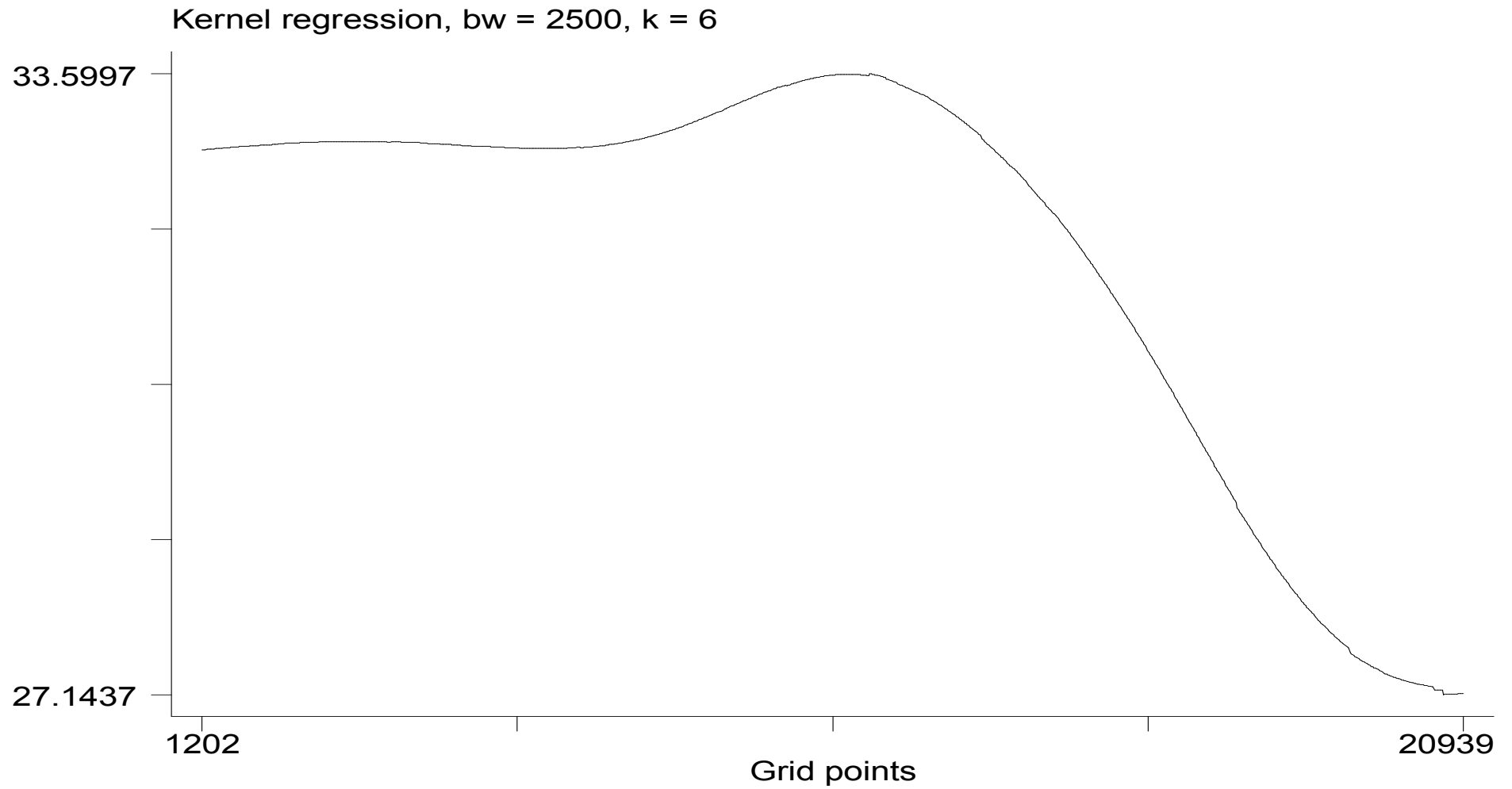
$$GINI = m(GDP) + \varepsilon$$

$$P20 = m(GDP) + \varepsilon$$

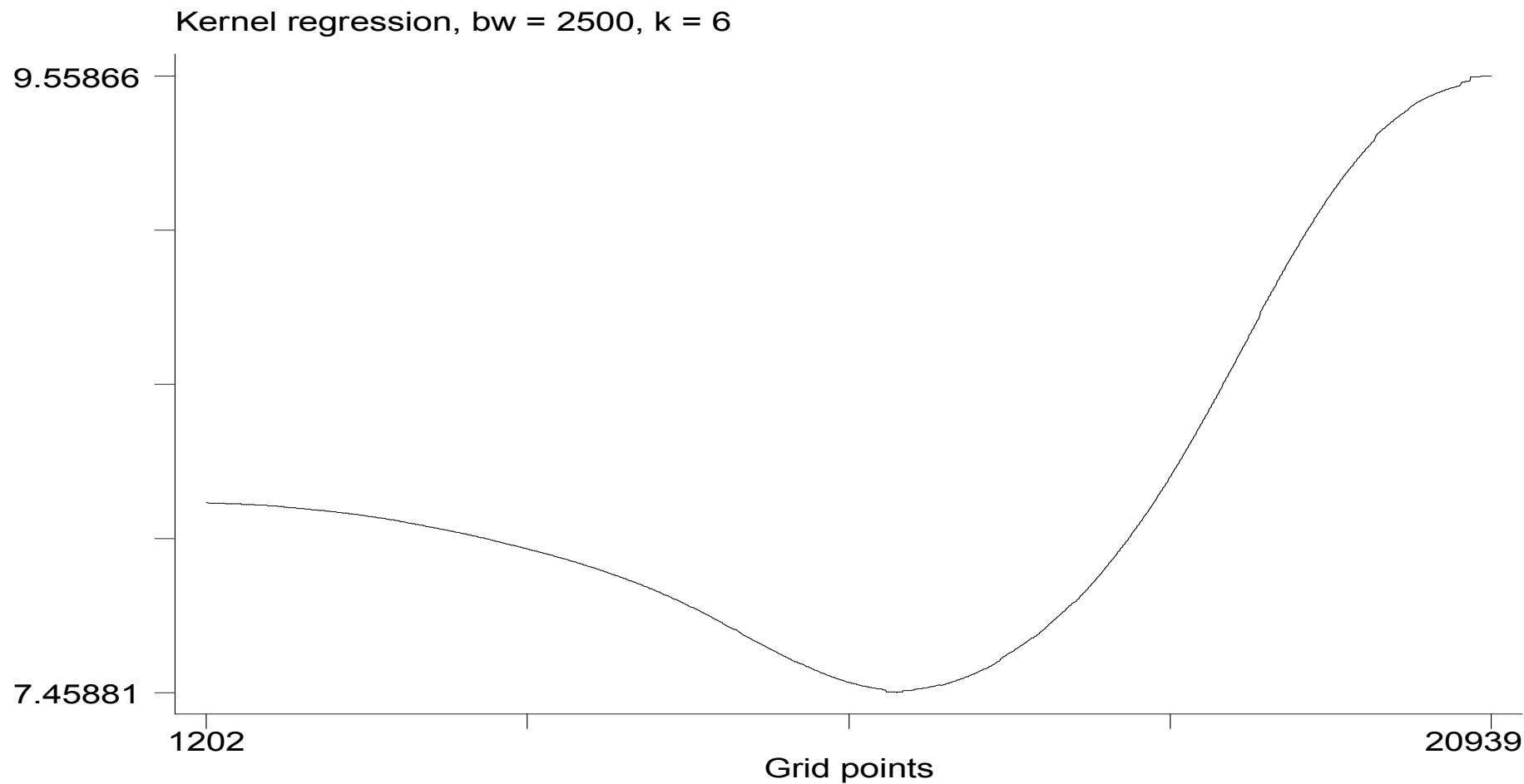
$$X20 = m(GDP) + \varepsilon$$

**The conditional expectation function,  $m(\dots)$  was estimated using the Nadaraya - Watson nonparametric regression with Gaussian kernel.**

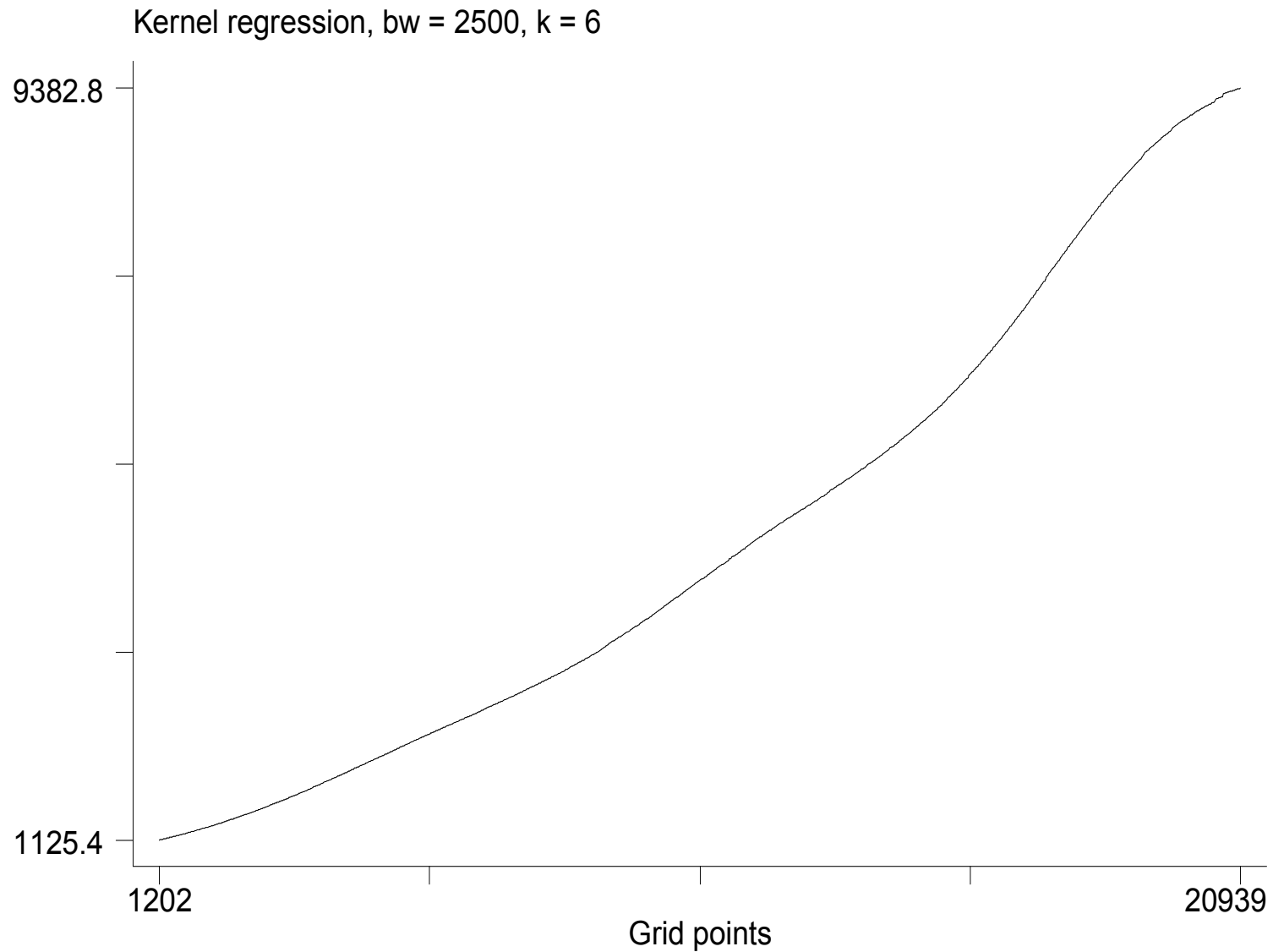
# The estimated conditional mean of the Gini index on per capita GDP



# The estimated conditional mean of the 20% low income share on per capita GDP



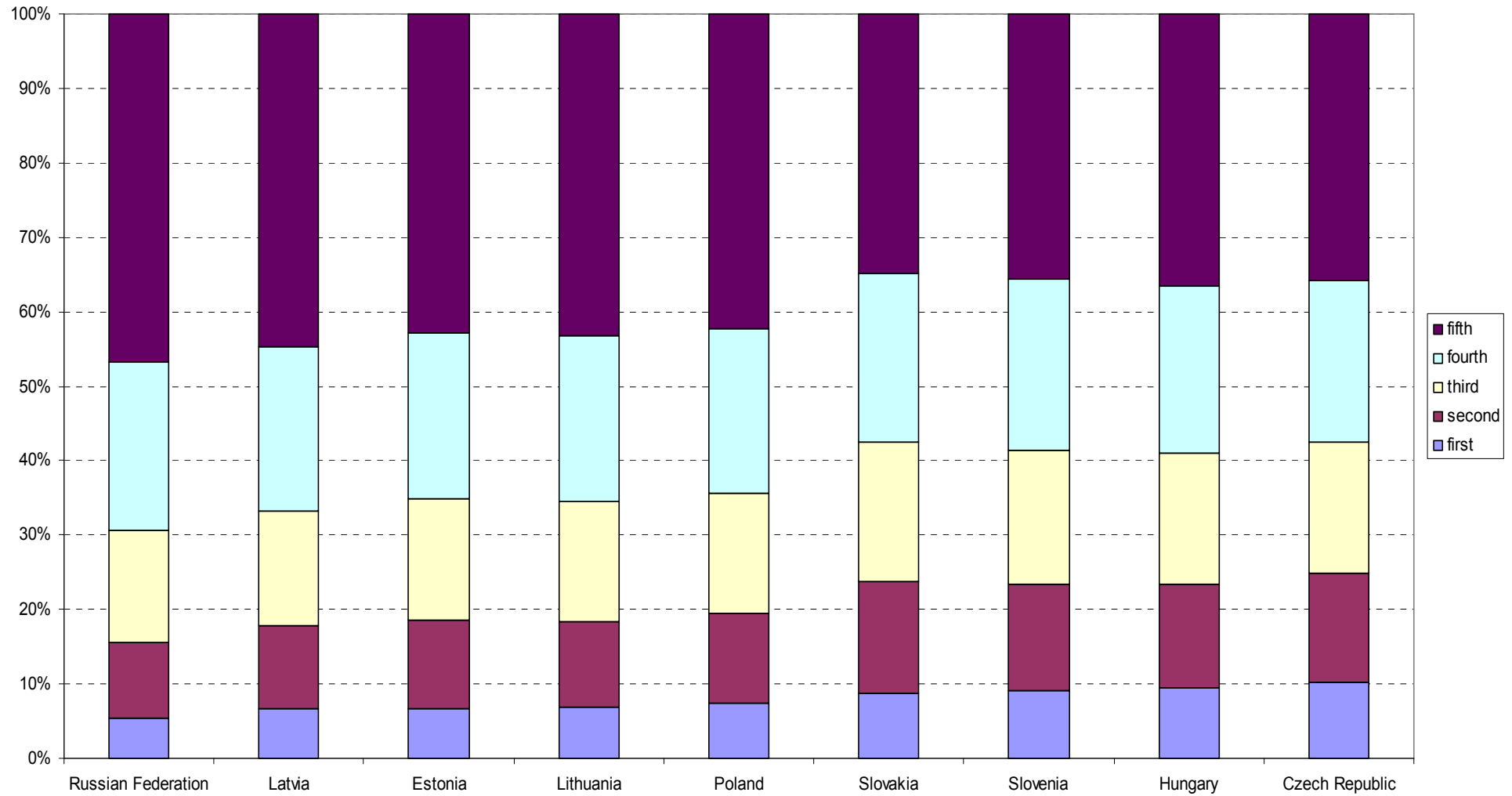
# The estimated conditional mean of the 20 % low income on per capita GDP



## Comparison Russian Federation with other countries

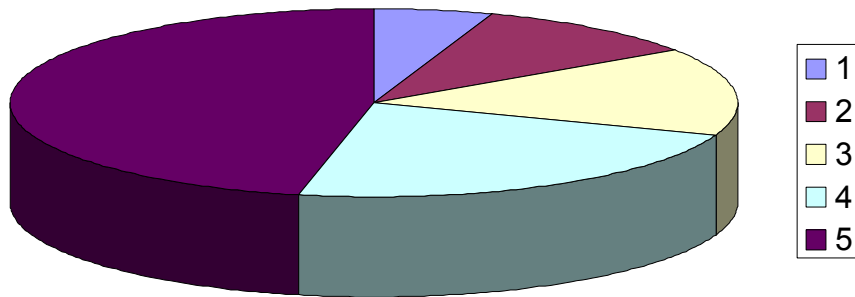
Country	GINI	GDP per capita			
			Belarus	29.7	6970
Tajikistan	32.6	1202	Bosnia and Herzegovina	26.2	7032
Moldova	33.2	1729	Kazakhstan	33.9	7440
Uzbekistan	26.8	1869	Bulgaria	29.2	8078
Kyrgyzstan	30.3	1935	Romania	31	8480
Lao People's Dem. Rep.	34.6	1954	<b>Russian Federation</b>	<b>39.9</b>	<b>9902</b>
Viet Nam	37	2745	Latvia	37.7	11653
Georgia	40.4	2844	Croatia	29	12191
Armenia	33.8	4101	Poland	34.5	12974
Azerbaijan	19	4153	Lithuania	36	13107
Turkmenistan	40.8	4584	Estonia	35.8	14555
Albania	28.2	4978	Slovakia	25.8	14623
China	44.7	5896	Hungary	26.9	16814
Ukraine	28.1	6394	Czech Republic	25.4	19408
Macedonia	39	6610	Slovenia	28.4	20939

# 20% shares of income

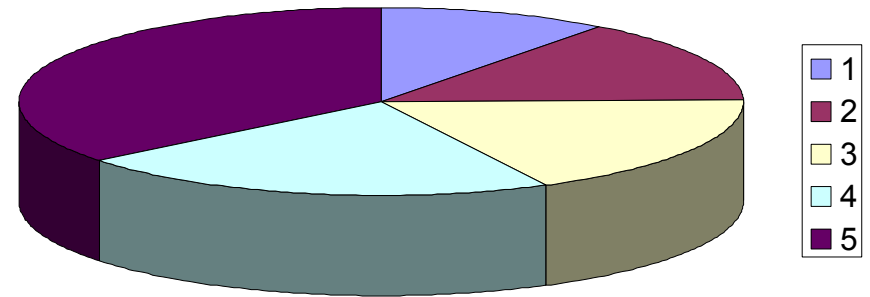


# Comparison income shares for Russian Federation and Czech Republic

## Russian Federation



## Czech Republic



## Conclusions

- **The drop in the Gini index after reaching the turning point is possible only with the low-income groups' income growth being ahead.**
- **The shape of the low-income groups' income dependence on the mean income after reaching the turning point must be convex.**
- **The data on 29 countries confirm the validity of the Kuznets hypothesis for transition countries.**
- **For this group of countries the turning point of ca. 11000 PPP USD was found.**
- **Among the countries with lower GDP per capita, Russia is the closest one to the turning point. We can expect reduction of the inequality level in this country with increasing GDP per capita.**





**Thanks  
for  
attention!**